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# Polynomials with all their roots on $S^1$

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## Abstract

We give a characterization of monic polynomials with coefficients in the ring of integers of a Galois number field having all of their roots on the unit circle. Such a characterization is given in terms of finitely many sum of powers of the roots of the considered polynomials.

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